Durability assessment of welded structures based on welding simulation with LS-DYNA®

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Abstract

The importance of welding for modern structural engineering cannot be emphasized enough. Different techniques are currently applied in the industrial environment offering almost unlimited possibilities regarding manufacturability with high cost effectiveness. At the same time the requirements on welded structures are increasing and so the requirements on the design methods. This paper presents an advanced calculation method for fatigue assessment of welds based on the simulation of a welding process in LS-DYNA®, thermophysical material modeling and fracture mechanics. The proposed method considers the most important aspects for durability prediction of welds. Applying worst-case assumptions, fatigue limits derived by the weight function method can be used in the lifetime assessment of complex welded structures together with the critical plane approach in order to consider a multiaxial nonproportional loading.

1 Introduction

Practical experience and experimental observations clearly show that fatigue damage in the welded structures generally originates from weld notches (toe or root). The fatigue behavior of the whole structure is therefore dominated by local stress concentrations in the vicinity of the welding fusion line, which is considered to be the weakest link. Apart from the purely geometrical weakening there are many other factors which may promote failure initiation in this area. During the arc welding, high thermal impact induces alterations in the microstructure and material properties of the weld metal and the surrounding heat affected zone. Surface conditions on the weld notch are typically poor, including many randomly distributed defects and small cracks, which can be seen as additional stress raisers. Moreover residual stresses are inevitably present after the welding as a result of plastic deformation induced by non-homogeneous thermal expansion, liquid-to-solid transformation and phase transformations in the solid state [1][2].

Welded structures can be very complex and involve many different types of welds, thus the accurate fatigue assessment becomes very demanding. Therefore, the biggest challenge for a product development in industrial environment is how to achieve a compromise between the accurate lifetime estimation and fast calculation procedure for the entire welded structure in order to be able to perform a design optimization in affordable amount of time. Design codes [3][4] can greatly reduce the analysis effort providing a suitable balance between computational accuracy and ease of use for many industrial applications. However the proposed S-N curve approach is rather generalized in respect of material or welding process. Various assumptions have to be made in a very conservative way so that the full cost and weight optimization potential cannot be achieved.

For less conservative fatigue estimation and a better design-to-cost a coupled analysis of welding process, operational loading and mechanism based failure modeling can be performed. Such a method starts at the extensive level of modeling of a welding process for prediction of microstructure, following by the micromechanical analysis of defects at the welding notch with help of the fracture mechanics. Finally the evidence from the detailed analysis (analog to the effective notch stress concept at IIW-recommendations), can be used to define a macroscopic criterion (analog to the structural hot spot stress concept at IIW-recommendations) for a large FE-model of entire structure. This approach would additionally offer a better understanding of interactions between welding and fatigue behavior and so more possibilities to optimize the welding process specifically for the considered material, weld type or loading.

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A good example of a heavily loaded welded structure is a low-speed 2-stroke marine diesel engine. Due to its enormous size the engine frame and the exhaust gas system are arc welded structures made of thick steel plates (Fig. 1). In case of the frame welds are subjected to a high frequent multiaxial non-proportional cyclic loading from combustion, propeller thrust and inertia of moving parts. Assuming engine lifetime of 30 years this structure must stand more than $10^9$ cycles and has to be designed against very high cycle fatigue (VHCF). In case of the exhaust gas system which consists of an exhaust gas receiver and a scavenge air receiver, weld seams are primarily loaded by the thermal expansion and the inner gas pressure. Therefore, the major loading cycle is represented by the engine’s start-stop, which is a low frequency loading and the structure must be designed in respect of low cycle thermo-mechanical fatigue (LCF, TMF). One should point here, that the bounds between different fatigue regimes are rather conditional and depend on many factors. In this work, the limit between VHCF and HCF is defined by the knee point on the S-N curve and is typically for steels around $10^9 \div 10^{10}$ cycles. LCF defines the area on S-N curve, where the loading leads to a notable plastic deformation of material and is below $10^4$ cycles.

Fig. 1. Major welded components on a 2-stroke diesel marine engine: engine frame and exhaust gas system (courtesy of Winterthur Gas & Diesel Ltd.).

2 Fatigue of welded joints

The fatigue nature for the majority of weld seams differs significantly from that of non-welded materials. In contrary to the fatigue investigations in laboratory conditions where welding quality can be well specified, it is difficult to make the detailed characterization for complex structures in industrial environment. A fatigue assessment therefore has to be done based on reasonable stochastically motivated assumptions containing the worst possible or worst allowable case in practice. Analysis of the fatigue resistance for welds therefore has to presume that cracks on weld seam are present after the welding process. In this case, the stage of a fatigue crack nucleation is relatively insignificant [5][6] and the threshold for the initial crack propagation can be taken as a criterion for VHCF whereas crack growth analysis can be used for HCF and LCF. Fig. 2 illustrates the differences between the S-N curves for welded and non-welded structures: while for non-welded metals with good surface condition and small size of inclusions a considerable amount of lifetime has to be spent for a crack nucleation, crack growth is dominant for welds.
Another reasonable assumption can be made regarding the location and the type of defects. Since weld notches are the highest loaded areas on a weld seam, one can assume that the surface crack-like defects are the most critical. This is proven by many years of field experience in marine industry and different investigations. For 2-stroke diesel engines the maximum allowable depth of cracks or crack-like flaws, identified by non-destructive testing, is 1 mm. Therefore, as the worst case, a semi-elliptical surface crack with a depth \( a \) of 1 mm and an aspect ratio \( a/c = 0.1 \) in the vicinity of the weld notch can be assumed as the most critical defect [3].

### 3 Welding simulation

An accurate fatigue assessment of weld seams requires information about residual stresses, microstructure and mechanical properties. Nowadays, the thermomechanical simulation of welding process can significantly facilitate this and provide more understanding of the relevant phenomena and their dependencies. However a reliable welding simulation is very demanding, not only in respect of calculation time but also regarding a comprehensive characterization of the material behavior [2]. Material models available in LS-DYNA® provide different possibilities for welding simulation [7]. In this study a semi-empirical temperature dependent elastic-viscoplastic material model with transformation kinetics based on Johnson-Mehl-Avrami-Kolmogorov and Koistinen-Marburger was used.

First, validation of the welding process simulation was performed on the 5-pass full penetration GMAW welding (Ø1.2 mm solid wire, CO2) on the single side clamped cantilever beams of steel S235JR with a width of 1000 mm (Fig. 3, a). During the welding process, the bending of the sample was restricted by clamps in order to simulate constraint in the real engine structure. After the welding, each of the 1000 mm long specimens was cut into 12 clamped samples for the cyclic bending fatigue tests (Fig. 3, b). Additionally measurements of the welding residual stresses were carried out using an X-ray diffraction technique. A microstructural and chemical analysis as well as hardness measurements at different areas of the weld seam were performed. For more information see [8] [9] [10].

![Fig. 3. a) clamped cantilever beams before welding; b) samples used in fatigue tests (courtesy of Winterthur Gas & Diesel Ltd.).](image-url)
convection, radiation and the contact with the clamping tools were considered. Fig. 4 shows the results of the thermal calculation in comparison to the measured temperature evolution at different locations and the weld pool geometry (red area represents a liquid state).

![Fig. 4. Comparison between measured and calculated temperature evolution (a) and the weld pool geometry (b).](image)

Since the thermal history during the welding is a crucial factor for microstructure and mechanical properties of the weld seam, it is possible to predict them already based on the fast thermal analysis. By exporting the cooling rate close to the notch of the last welding pass to the program JMatPro one can predict the final microstructure and therefore hardness of the material.

Fig. 5 shows the results of the predicted phase ferritic-bainitic phase composition and observed microstructure. The predicted hardness value of HV217 on the fusion line was very close to the measured value of HV213.

![Fig. 5. Comparison between the measured microstructure (b) and the prediction by JMatPro (a).](image)

Thereby, a relatively fast thermal simulation of the welding process is able to predict microstructure and so mechanical material properties at any location of the weld seam. In order to get welding induced residual stresses mechanical analysis has to be performed.

### 3.2 Mechanical analysis and residual stresses

In the mechanical analysis, the elastic-viscoplastic temperature dependent material behavior including the phase dependent dilatation and the transformation-induced plasticity has to be considered. One of the twelve fatigue specimens was extracted from the middle of the model for a comparison of
measured residual stresses. Fig. 6 shows measured and calculated residual stresses in longitudinal (parallel to the weld seam) and transversal direction on the upper side of the specimen.

![Image showing measured residual stresses](image)

**Fig. 6. Comparison between measured and calculated residual stresses in longitudinal and transversal direction on the upper notch.**

Welding induced residual stresses can have either a beneficial or a harmful effect on the lifetime, depending on sign, magnitude and distribution with respect to the load-induced stresses. Typically tensile residual stresses reduce the fatigue resistance of components by assisting the fatigue crack growth while compressive residual stresses decrease it. Using available commercial software for welding simulation, it is often difficult, without extensive material characterization, to estimate accurately the welding induced residual stresses even for idealized boundary conditions at laboratory or for simple geometries. For many real welded structures with complex geometry and welding sequence, local stress state on the welding notch can be additionally affected during the assembling stage. Another aspect, which has to be taken into account if welding residual stresses need to be considered in the fatigue analysis, is their alternation during the cyclic loading or at high temperature.

All mentioned above difficulties related to the accurate calculation of residual stresses, make it currently impossible (at least quantitatively) to use the information for lifetime prediction of complex structures. For the derivation of macroscopic fatigue limits therefore, stress ratio $R=0.5$ seems to be a reasonable conservative assumption.

### 4 Fatigue crack analysis

Due to the presence of weld notches, the through-thickness stress has a nonlinear distribution and classic analytical solution for the stress intensity factors is no longer valid. An accurate solution by using FE-analysis is can be very time consuming. Convenient and efficient is in contrast the weight function method. The weight function can be understood as the stress intensity factor induced by the simplest load configuration, i.e. a pair of unit splitting forces attached to the crack surface. For the fatigue analysis, range of the stress intensity factor for semi-elliptical surface crack subjected to Mode I loading can be obtained by integrating the product of the stress distribution $\Delta \sigma(x)$ in the anticipated crack plane and the weight function $m(x,a)$ along the crack length $a$ [11]:

$$\Delta K_{A,B} = \int_0^a \Delta \sigma(x)m_{A,B}(x,a)dx$$  \hspace{1cm} (1)

where $A$ and $B$ are points on the crack front (Fig. 7). According to [12], conservatism of the weight function method can be provided up to the crack depth of 80% of the plate thickness.
For the calculation of stress intensity factors by the weight function method, information about stress distribution along the crack front and the potential crack path is essential. In a typical structure with different weld seams, complex geometry and loading, various through-thickness stress distributions are possible. In order to perform fatigue assessment for complex parts in a reasonable amount of calculation time a worst-case assumption in regards to the through-thickness stress distribution can be made. Assuming Mode I as a dominant for crack growth, the most critical stress state is the one with the highest range of the maximum normal stress, means where the entire section is under the tension. In order to study the effect of plate thickness on stress distribution a parametric FE-analysis was performed [10] using a 2D plane strain model for plate thicknesses varying from 10 to 50 mm (Fig. 8, a). The effect of misalignment was not included and the flank angle of the weld was 45 degrees. The radius on the weld toe initially was chosen to be 1 mm which corresponds to the effective notch stress concept [3]. Stress distribution is normed by the peak stress \( \sigma_{\text{peak}} \) over the normed plate thickness coordinate \( x/t \). The anticipated crack growth path is normal to the plate thickness and starts at the point with the maximum stress on the notch surface.

Furthermore, the radius affects to the gradient of the stress concentration (Fig. 8, a). The smaller radius the higher is the peak stress. If the initial crack size is large compared to the depth of the stress gradient, i.e. the initial crack size covers the steepest stress gradient, the radius of the weld toe does not affect significantly the crack growth rate in depth direction. For the case of the initial crack depth of 1 mm, the influence of the notch radius size (0.5 mm or 1 mm) on the crack propagation in the depth direction is therefore assumed negligible.

As can be seen from Fig. 8, when plate thickness increases, the stress concentration becomes shallower compared to the plate thickness. This means that the stress concentration factor is higher for thick plates. The dimensionless distribution can be described e.g. by exponential law as a function of the plate thickness in the following form:

\[
\Delta \sigma(x) = \Delta \sigma_{\text{peak}} \cdot f(x/t)
\]  

\( f(x/t) \)
From Eqs. (1) and (2) one can get the range of the stress intensity factor as a function of the peak stress range:

$$\Delta K_{A,B} = \Delta \sigma_{\text{peak}} \int_{0}^{a} f(x,t) m_{A,B}(x,a) dx$$  \hspace{1cm} (3)

For the sake of simplicity linear elastic fracture mechanics (LEFM) is considered in this study. This is legitimate for our case where the initial size of the surface crack is larger than 0.5 mm and belongs to the long crack range \([8][9]\).

### 4.1 Very high cycle fatigue

Flaws and crack-like defects on weld seams can propagate under fatigue loading if the stress intensity factor is above its threshold value \(\Delta K_{th}\). If \(\Delta K\) is below that value, theoretically infinite fatigue life can be obtained. Murakami [15] proposed a simple relation that predicts the fatigue crack propagation threshold for small initial defects (short crack range) \(\Delta K_{th}^{\text{short}}\) at the loading ratio \(R_K = -1\) assuming the crack opening mode, or Mode I, as the dominant. He found a correlation between the material hardness \(H_V\), the effective area of the defect projected onto the plane normal to the first principal stress, \(\sqrt{\text{area}}\), and the fatigue strength:

$$\Delta K_{th}^{\text{short}} = 3.3 \times 10^{-3} (H_V + 120)(\sqrt{\text{area}})^{1/3}$$ \hspace{1cm} (4)

where \(H_V\) is a Vickers hardness in kgf/mm\(^2\), \(\sqrt{\text{area}}\) in \(\mu\text{m}\) and \(\Delta K_{th}^{\text{short}}\) in MPa\(\sqrt{\text{m}}\).

Eq. (4) has been successfully validated for different classes of materials. However, it is only defined for the short cracks. For the long crack range it is no longer valid [16]. In order to extend the applicability of Murakami’s model, Chapetti [17] proposed the upper bound for the Eq. (4):

$$\Delta K_{th}^{\text{long}} = -0.01239 H_V + 15.5$$ \hspace{1cm} (5)

Combination of (4) and (5) provides the general threshold value:

$$\Delta K_{th} = \min \left[ \Delta K_{th}^{\text{short}}, \Delta K_{th}^{\text{long}} \right]$$ \hspace{1cm} (6)

The mean stress sensitivity which includes effect of residual stresses and loading asymmetry over one cycle can be described by different models. Using experimental data for steel St 37 (former designation for S235) from [4] a very accurate approximation can be achieved by the following function of the mean stress intensity factor \(K_m\):

$$\Delta K_{th} = \Delta K_{th0.5} + \frac{\Delta K_{th1} - \Delta K_{th0.5}}{1 + a_k e^{K_m}}$$ \hspace{1cm} (7)

where \(a_k\) and are material parameters. Fig. 9 presents the description of measured values with \(a_k = 0.001\). The values at \(R_K = -1\) \((R_K = K_{\text{min}}/K_{\text{max}})\) were predicted by Eq. (6) based on \(R_m = 415\text{MPa} \ (R_m = 3.26 H_V)\). Stress intensity factor ratio, \(R_K\), is defined as:
Fig. 9. Mean stress dependency for steel St 37: experimental values and described by Eq. (7).

Using the information about the through-thickness stress distribution and shape of the surface crack, fatigue limit can now be derived by the weight function method. Substituting the range of stress intensity factor on the left side in (3) by its threshold value (7) one can derive a limit for stress range in VHCF regime:

\[
\Delta \sigma_{wR}^{\text{VHCF}} = \frac{\Delta K_{\text{th}}}{\text{max} \left\{ \int_0^{a_0} f(x,t) m_A(x,a) \, dx, \int_0^{a_0} f(x,t) m_B(x,a) \, dx \right\}}
\]

where \( a_0 \) corresponds to the initial crack length. In this case the fatigue limit is related to the peak stress on the notch surface.

4.2 High and low cycle fatigue

For regimes of the high and low cycle fatigue, \( \Delta K \) from external load exceeds its threshold value and crack growth up to its critical size (specified by the structural requirements) must be modeled in order to predict lifetime. In terms of LEFM crack growth in the direction normal to plate surface can be described by the Paris law:

\[
\frac{da}{dN} = C (\Delta K)^m
\]

where \( N \) is a number of loading cycles, \( C \) and \( m \) are the material constants. In this simple form it is not able to consider effect of the loading ratio as well as a crack closure on crack growth rate. However, for industrial applications it is sufficient to assume a constant high \( R \)-value due to the following reasons: difficulty in prediction of residual stress distribution and their relaxation for complex structures, inability to consider local stress redistribution during the crack propagation, high gradients of material properties along the anticipated crack path.

The total life can be calculated as:

\[
N = \frac{1}{C} \int_{a_f}^{a_0} \left( \frac{da}{(\Delta K)^m} \right)
\]

where the criterion for failure can be defined by fracture toughness \( K_{fc} \) and the critical crack size \( a_f \), specified e.g. by validity of the Glinka’s weight function method \( a_f = 0.8 \, t \).

Combining Eqs. (3) and (10) one can derive the allowable stress range for the HCF and LCF regimes:
4.3 Multiaxiality and non-proportionality of loading

Until now, stress acting normal to the crack plane is considered, because of the Mode I assumption. Real welded structures however have a random orientation of initial defects and are typically subjected to a complex loading. For a general case of a multiaxial and non-proportional loading [18], one can formulate the fatigue criterion based on the critical plane approach as follows:

\[
D = \frac{\max_{\phi, \theta} [\Delta \sigma_n]}{\Delta \sigma_{n,R}} \leq 1
\]

where \( D \) is fracture parameter, which represents a ratio between the maximum value of the normal stress range \( \Delta \sigma_n \) over all plane orientations, defined by spherical coordinates \( \phi \) and \( \theta \), and a fatigue limit. If residual stresses are not known, a conservative assumption regarding the \( R_K \)-value has to be made (e.g. \( R_K = 0.5 \) according to [3]).

Accurate simulation with critical plane method requires small angular step and can lead to very high calculation times. For complex structures calculation times can be reduced if only planes which are parallel to the welding fusion line (\( \theta = 0^\circ \)) are considered. For even faster analysis the first principal stress range defined as a function of ranges of each stress component can be used for calculation of the maximum normal stress. In case of the plane stress state, e.g. on the plate surface:

\[
\Delta \sigma_n = \frac{\Delta \sigma_{11} + \Delta \sigma_{22}}{2} + \sqrt{\left(\frac{\Delta \sigma_{11} - \Delta \sigma_{22}}{2}\right)^2 + \Delta \sigma_{12}^2}
\]

Eq. (13) presumes that the maxima and the minima for each stress component occur simultaneously and the loading is proportional.

4.4 Fatigue life prediction

Based on the theory and assumptions presented above as well as on the results from the welding simulation one can now derive an S-N curve for S235JR. Validation of the results is done by the fatigue limits from IIW. For that purpose the effective notch stress concept can be chosen. FAT 225 represents a survival probability of 97.7% at stress ratio \( R = 0.5 \). Since FAT 225 provided above can be used. For the calculation of crack growth material constants from [4] for S235JR (base material) at \( R = 0.5 \) were used: \( C = 9.71 \times 10^{-9} \) and \( m = 2.71 \) (units: MPa, m). For the calculation of the stress intensity threshold hardness HV213 was taken. Plate thickness was selected to be 10 mm. Resulting S-N curve compared to the one from IIW can be seen on Fig. 10. As mentioned before, LEFM presumes an existence of the endurance limit defined by the stress intensity threshold, which is however disputed in the fatigue world. Therefore \( \Delta K_{th} \) is used here only for estimation of the knee point on S-N curve. For the number of cycles higher than at the knee point, a further decline in stress range of 10% per decade is assumed [3].
Fig. 10. Fatigue limits for welds from IIW and predicted by the crack growth calculation.

Fig. 11 presents evolution of stress intensity factors at position A and B as well as crack dimensions (for notation see Fig. 7) during the crack growth loaded by $\sigma_{\text{peak}} = 1000$ MPa.

Fig. 11. Development of stress intensity factors (a) and crack dimensions (b) during the crack growth.

In opposite to IIW, predicted by the presented here approach limits can be derived for particular material, welding process and stress state. This provides more additional possibilities for design and process optimizing. Fig. 12 shows predicted fatigue limits (defined by knee point) for the same material by variation of hardness and initial flaw size.

Fig. 12. Fatigue limits as a function of hardness (a) and initial crack size (b).

It can be seen, that there is still a lot of potential regarding the optimization of welding process. Such as reducing material hardness at the notch area to the level of HV150 would increase fatigue limit by almost 10%. This can be achieved by reduction of cooling rate - either by reduction of the heat input during the last welding pass or by pre-heating of the welding area. Any further increase of the cooling rate would lead to more brittle microstructure and as sequence to the reduction of fatigue strength. Even more improvements can be achieved with increase of the welding quality. Reduction of the initial depth of the surface crack to 0.4 mm will provide fatigue limit of 186 MPa – an increase by 28%.
4.5 Application for complex structures

Derived by the proposed approach limits can now be used for the fatigue assessment of complex welded structures. In order to reduce calculation time, fatigue limits can be defined as a function of plate thickness and temperature. All other factors, including through-thickness stress distribution, can be first considered based on the worst-case assumptions. Since the component size is typically much bigger compared to the size of weld seams and notches, they are not included in the FE-model and the mesh size is coarser than the one for the effective notch stress concept. For this case, fatigue limits derived by LEFM-approach must be scaled accordingly. Mesh requirements as for the structural hot spot concept [3] can be applied. Fig. 13 presents calculated by Eq. (14) fracture parameters for the engine frame, which is loaded in VHCF regime at room temperature. Using simplified approach (15) for the maximum normal stress, the post-processing time for calculation of the fracture parameter $D$ takes only a few seconds.

![Fracture parameter D](image)

Fig. 13. Fatigue analysis of complex welded structures: engine frame – VHCF at room temperature (courtesy of Winterthur Gas & Diesel Ltd.).

5 Conclusions

The emphasis throughout this study has been to formulate and validate an accurate approach for the fatigue life assessment of welded joints, in order to achieve the full cost and weight optimization potential for industrial applications. The proposed method starts at the extensive level of modeling of a welding process. Thermomechanical welding simulation assisted by metallurgical material modeling is able to predict the microstructure, mechanical properties and the welding induced residual stresses. Using this information lifetime of weld seam can accurately be estimated by the weight function method associated with threshold for crack propagation and crack growth rate. Derived by this method fatigue limits in combination with the critical plane approach can successfully be used in the analysis of complex parts subjected to a multiaxial and non-proportional loading. The capability of the approach is validated by S-N curves provided at the IIW-recommendations [3].

6 References


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