

A Distributed Randles Circuit Model for Battery Abuse Simulations Using LS-DYNA®

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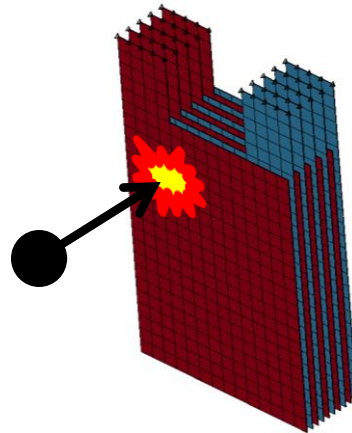
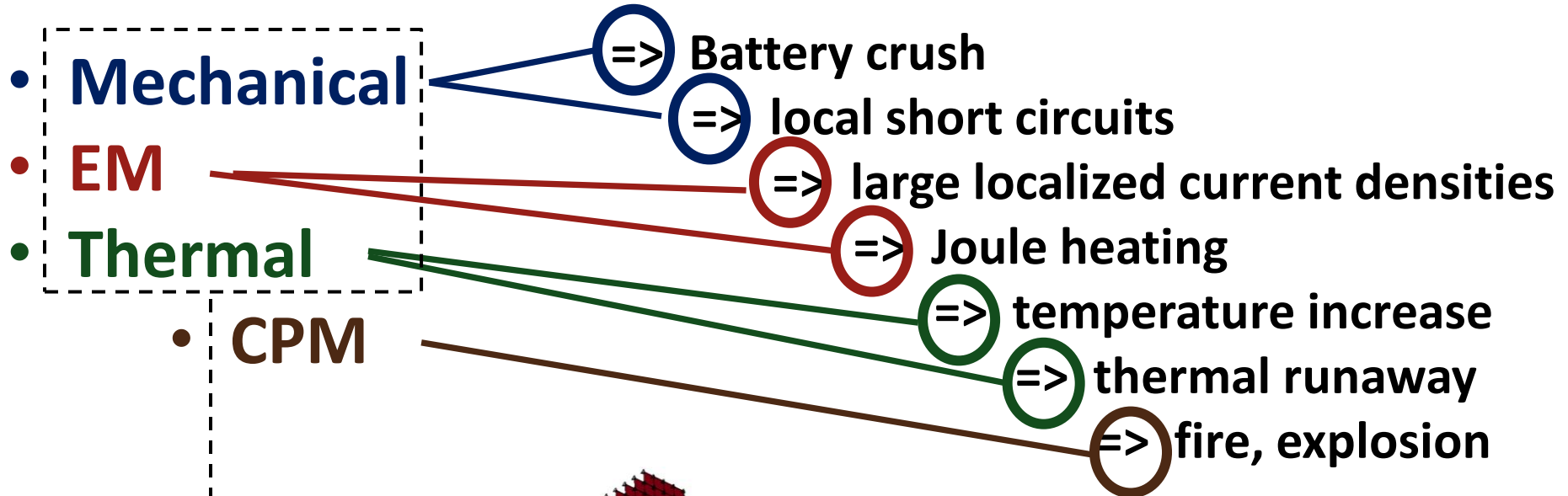
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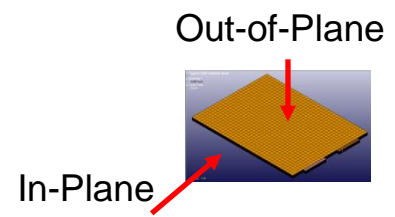
Car crash



Case Study Development Assumptions

	Crash	Regulatory Crush	Overcharge/External Short/Thermal Ramp
Mechanics Time Scale	< 100 ms	> 10 s	> 10 s
EM/thermal Time Scale	ms to minutes		
Deformation Mode	Out-of-Plane or In-Plane Compression; Bending; Shear	Out-of-Plane Compression; In-Plane Compression	Internal Swelling; Separator Melting
Solver Assumption	Explicit to Implicit	Implicit	Implicit

- 3-D, transient finite element code needed to span these target applications
- Models that resolve mechanical properties of individual layers have higher potential robustness to multiple deformation modes



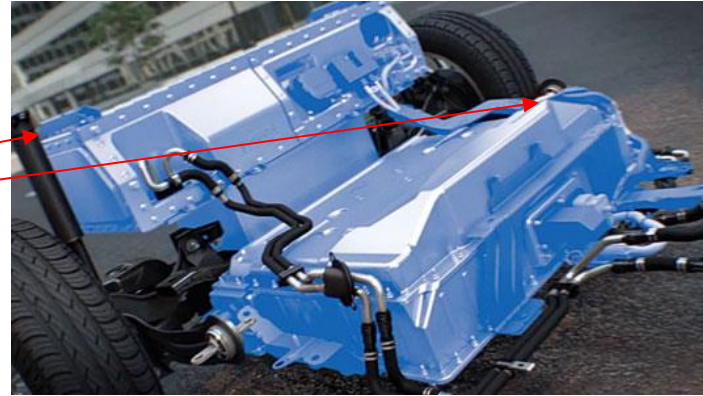
- Li-ion cell in an electric car
- The distributed Randles circuit model
- Validation on various electrical cycling experiments (“benign” use)
- Presentation of external short cases
- Presentation of internal short cases

Li-ion cell

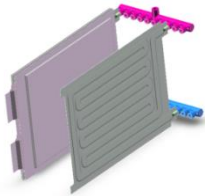
Vehicle



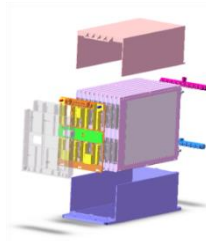
Dual-Packs



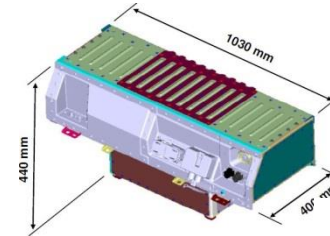
Cell



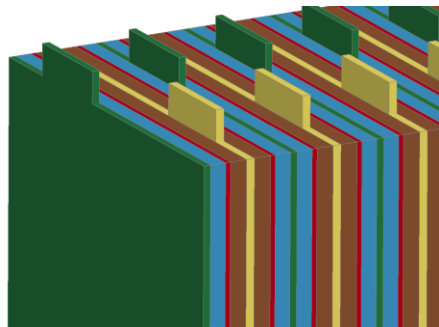
Module



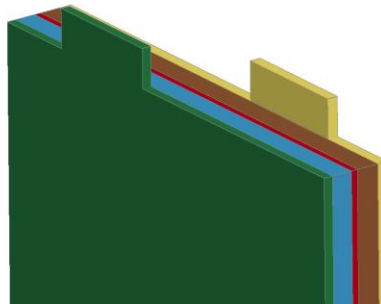
Pack



Cell (zoomed in z)



Unit cell (zoomed in z)



180 μ m

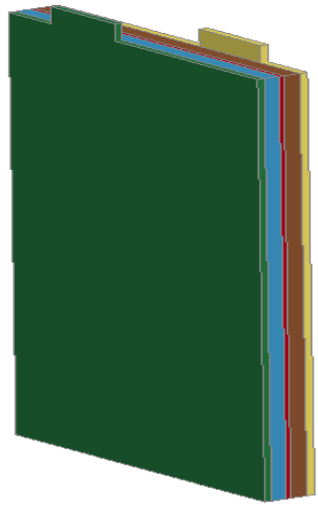
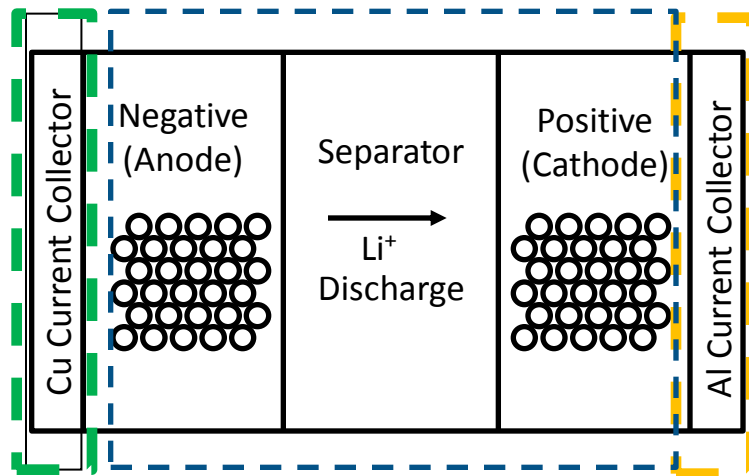
20cm

15cm

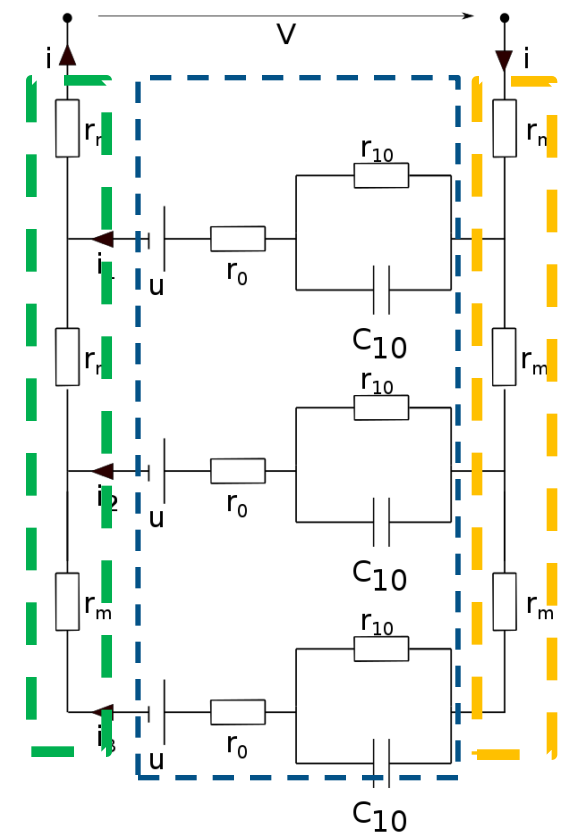
- Li-ion cell in an electric car
- **The distributed Randles circuit model**
- Validation on various electrical cycling experiments (“benign” use)
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- Presentation of internal short cases

Distributed Equivalent Circuit

(1st Order Randles)



- Current collectors transport electrons to/from tabs; modeled by resistive elements
- Jelly roll (anode – separator – cathode) transports Li⁺ ions; modeled with Randle circuit



r_0 : Ohmic & kinetic
 r_{10} & c_{10} : Diffusion
 u : Equilibrium voltage (OCV)
 r_m : Current collectors



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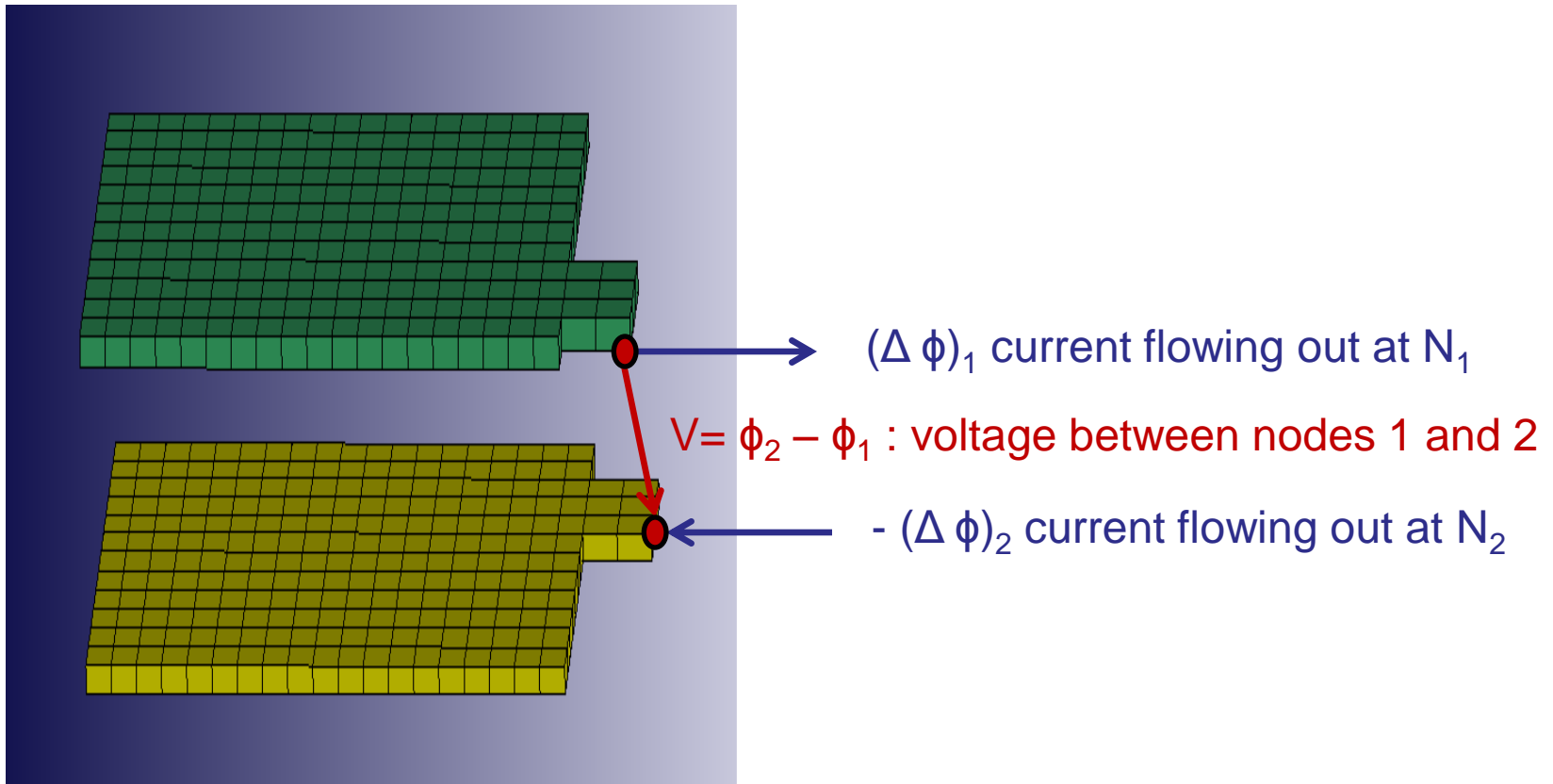
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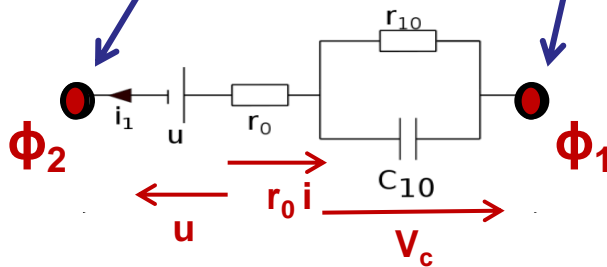
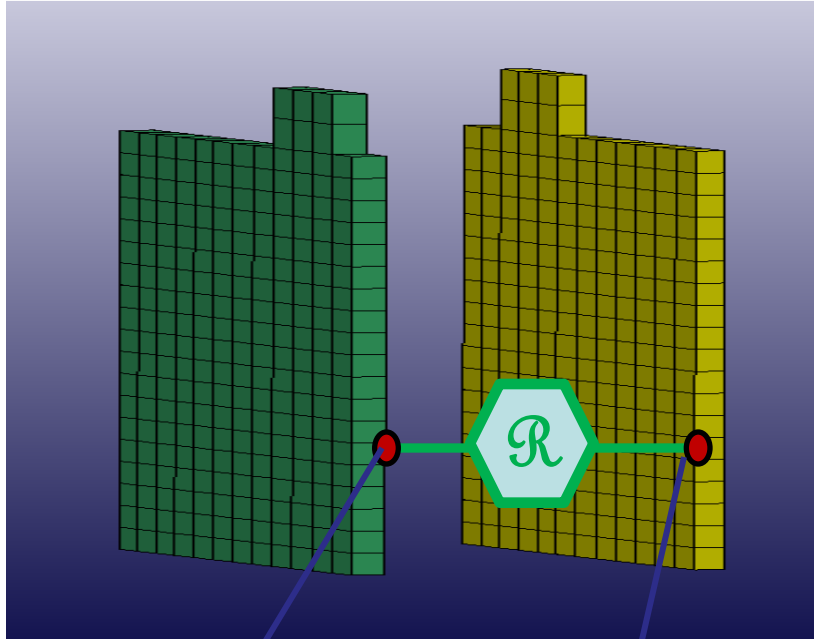
Standard EM resistive solver



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- ϕ : potential
- $E = -\text{grad}(\phi)$: electric field
- $V = \phi_2 - \phi_1$: voltage
- $J = \sigma E$: current density (σ = electric conductivity)
- $\text{div}(J) = 0 \Rightarrow \Delta \phi = 0$ + boundary conditions





Randle circuit

$$\begin{aligned}\phi_2 - \phi_1 &= u - r_0^*i - V_c \\ r_0^*i + \phi_2 - \phi_1 &= u - V_c \\ i + (\phi_2 - \phi_1) / r_0 &= (u - V_c) / r_0\end{aligned}$$

FEM solve:

$$(S_0 + D) * \phi = b$$

Where

- S_0 is the Laplacian operator (nds x nds)
- D has
 - $1/r_0$ at (N_1, N_1) and (N_2, N_2)
 - $-1/r_0$ at (N_1, N_2) and (N_2, N_1)
 - 0 elsewhere
- b has
 - $1/r_0(u - v_c)$ at N_1
 - $-1/r_0(u - v_c)$ at N_2
 - 0 elsewhere

Actualization of randle circuits:

$$i = (S_0 * \phi)(N_1)$$

$$V_c(t+dt) = V_c(t) + dt * (i/c_0 - V_c(t)/r_{10}/c_{10})$$

$$\text{soc}(t+dt) = \text{soc}(t) - dt * i * c_Q / Q$$

$$u = u(\text{soc})$$



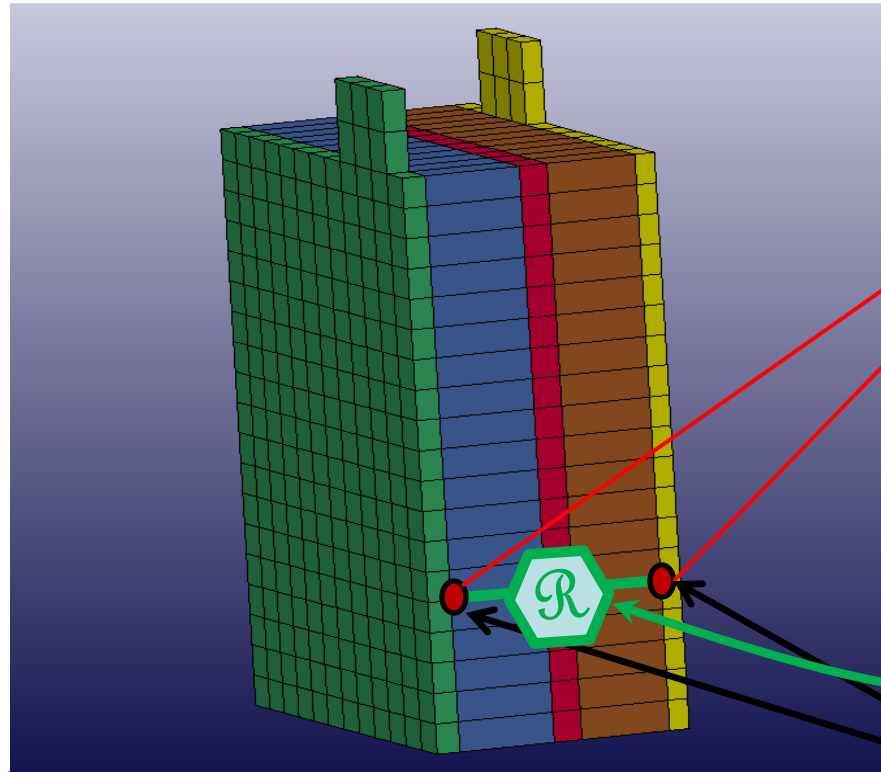
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EM/thermal connection

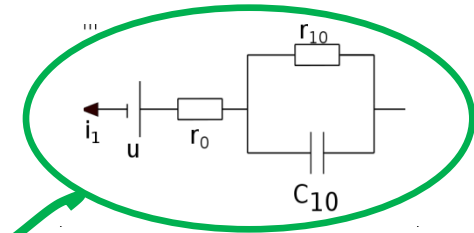


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**T from thermal for
 r_0, r_{10}, C_{10} vs T**

Randle circuit



**$r_0 * i^2$ added to thermal
ITdU/dT added to thermal**

Cu collector : EM+Thermal **Al collector : EM+Thermal**

Anode : Thermal **cathode : Thermal**

Separator: Thermal

**Allow correct material mass,
heat capacity and thermal conductivity**



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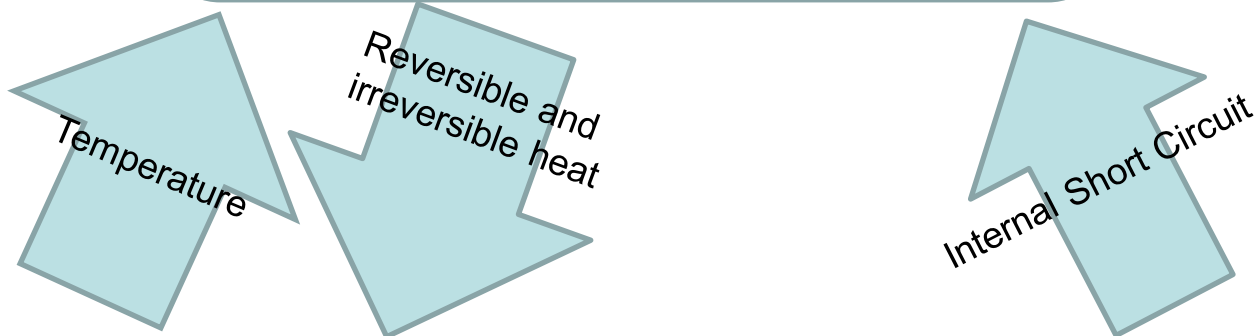
EM/thermal/mechanical connections



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Electrochemical

- Ordinary differential equations (Randles circuit model)
- Finite element analysis



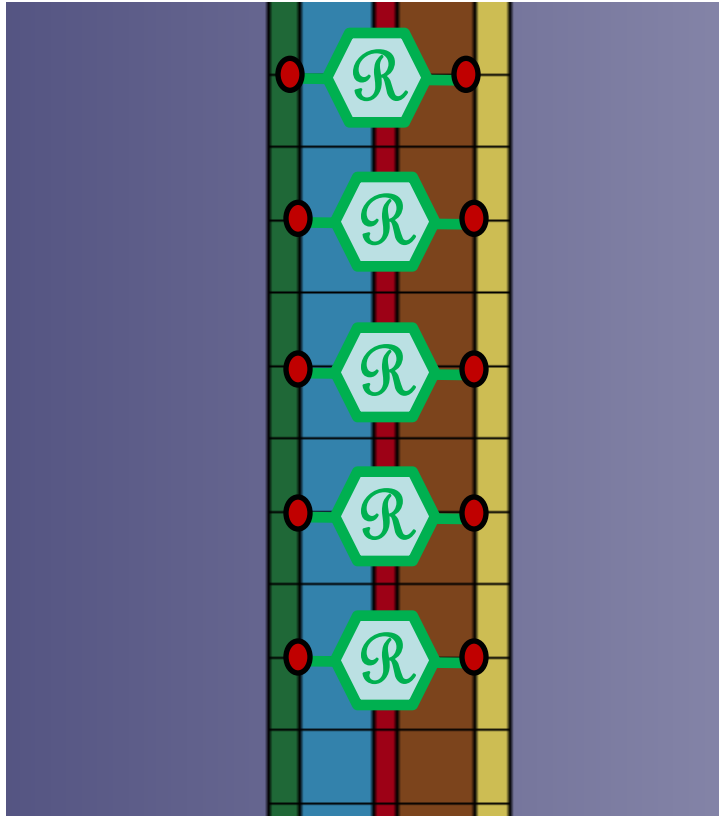
Thermal

Finite element analysis;
3-D Heat diffusion with source terms

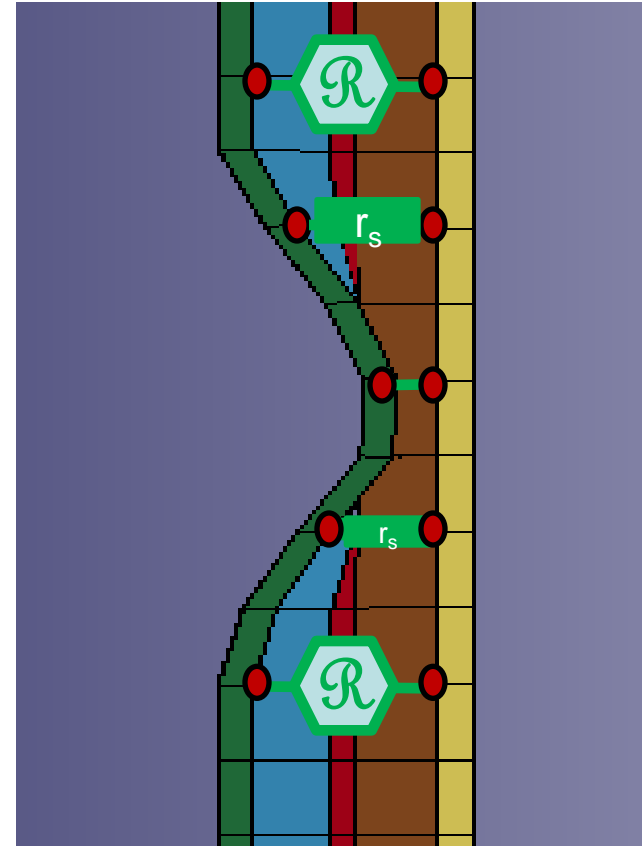
Structural

Finite element analysis;
Nonlinear continuum mechanics

Contact for Internal Short Models



Replace randle circuit by resistance r_s
 $R_s * i^2$ added to thermal



Experiment + simulation
(voltage, current, temperature)
should give good models



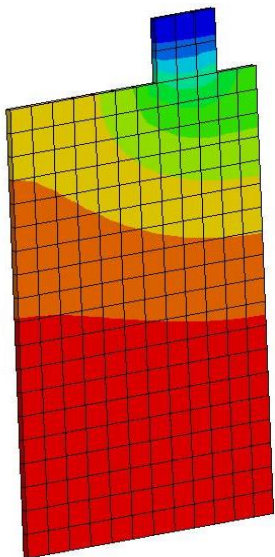
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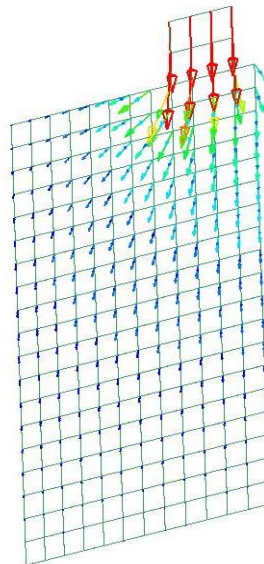
Randle circuits in LS-PREPOST



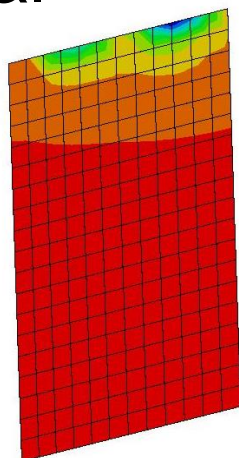
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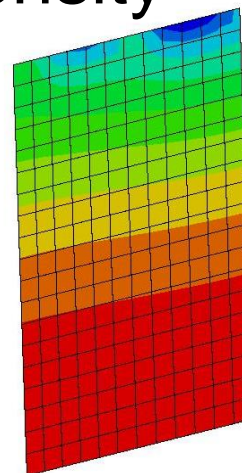
Scalar potential



Current density



Randle r0



Randle SOC



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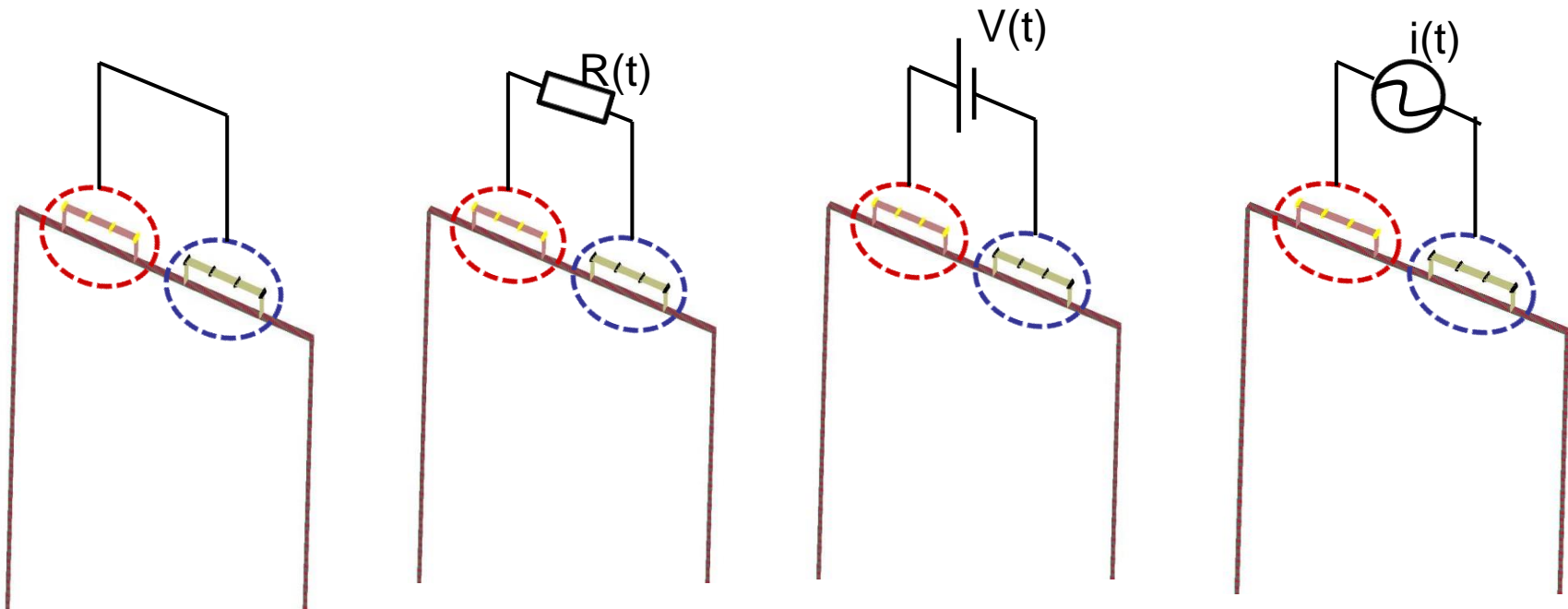
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Connection to external circuits



Isopotentials can be defined and connected:

- The connectors do not need to be meshed.
- Enables alignment of cell simulations with experimental conditions (low rate cycling, HPPC, continuous discharge, ...).



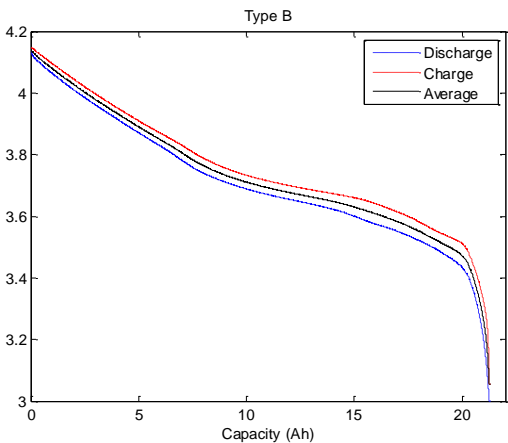


Evaluation of the circuit parameters

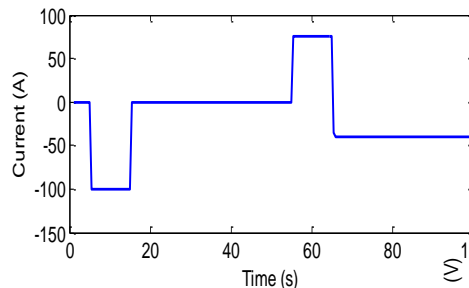


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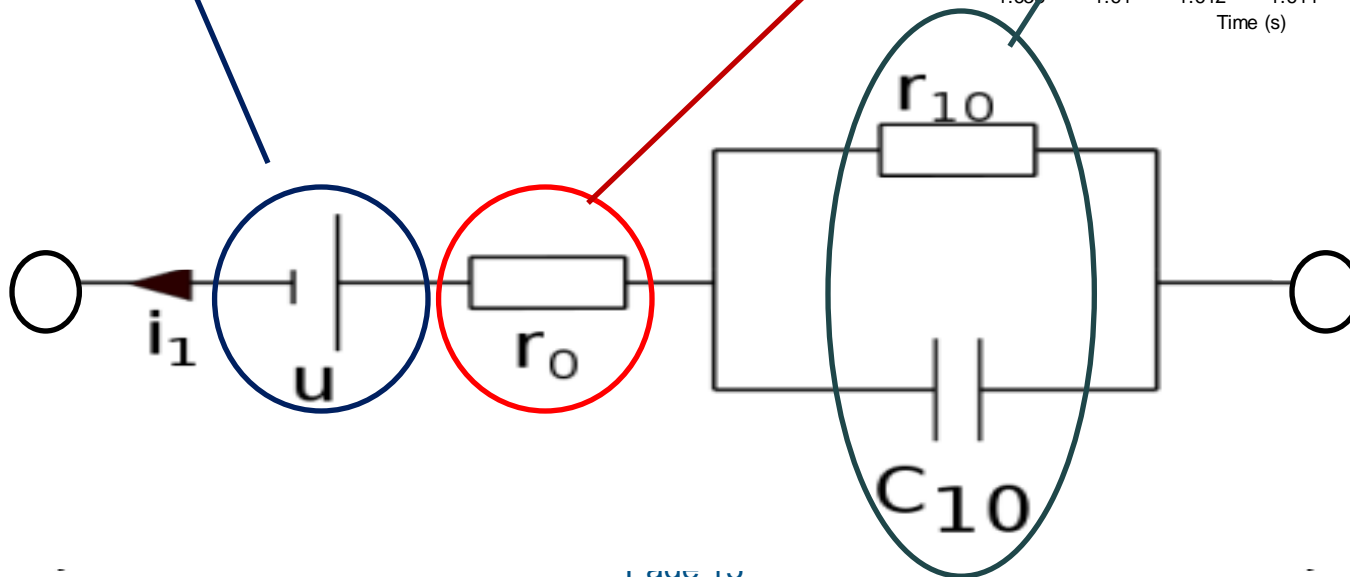
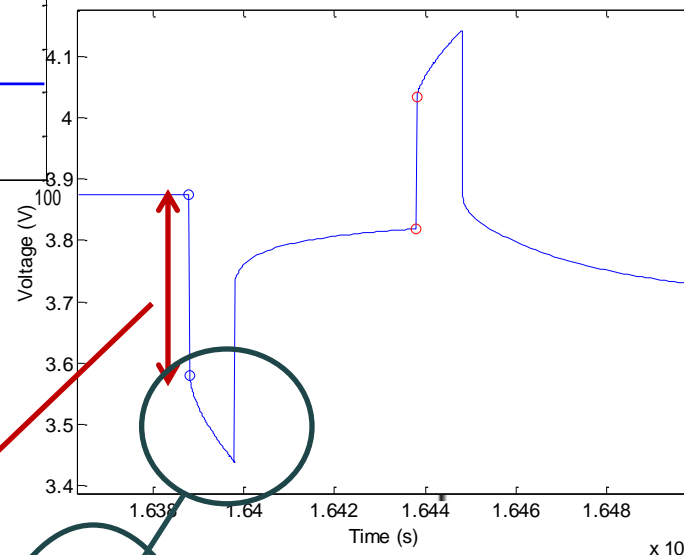
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C/10
capacity tests



HPPC tests



- Li-ion cell in an electric car
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- **Validation on various electrical cycling experiments (“benign” use)**
- Presentation of external short cases
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Benchmarking with experimental results

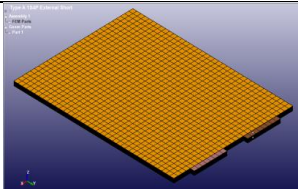
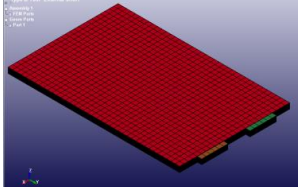
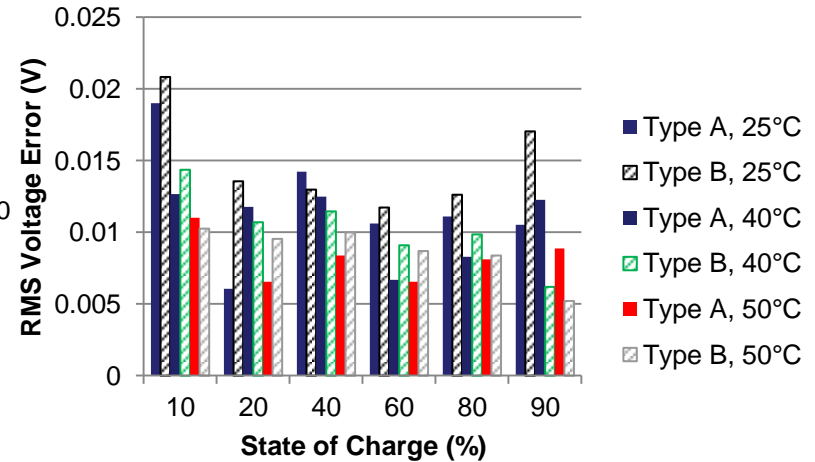
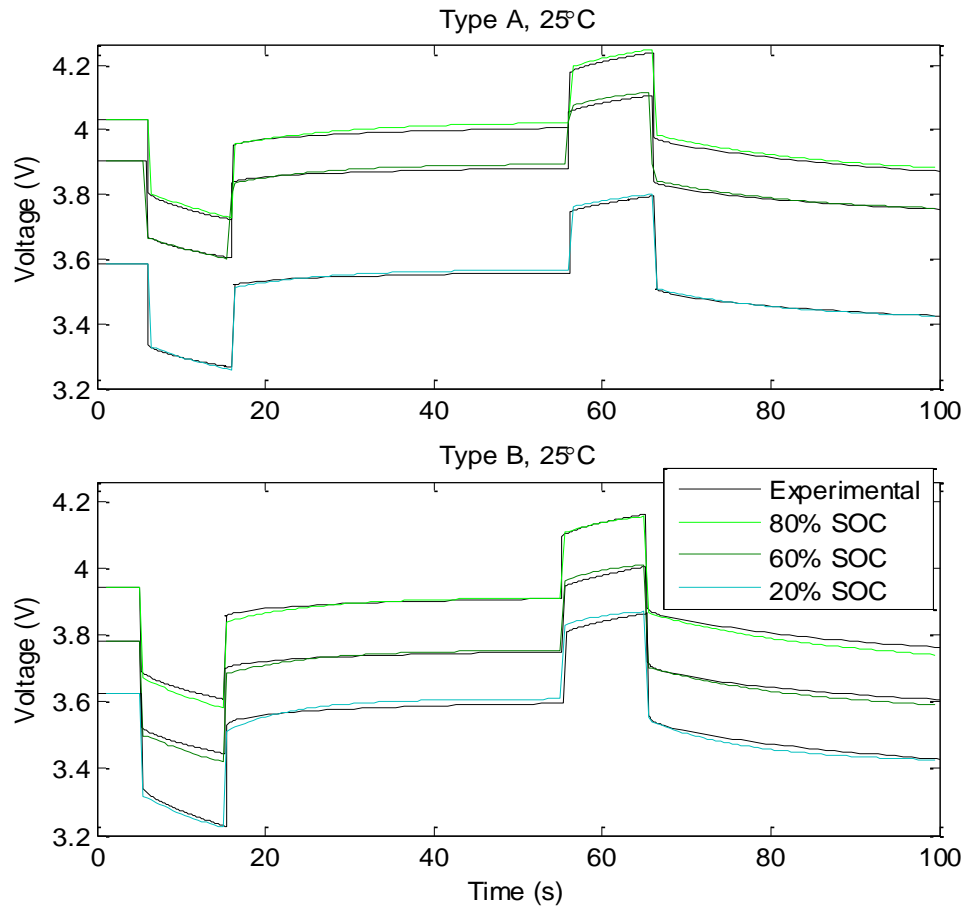
Image	Type	Cathode Chemistry	Dimensions	Number of Elements
	A	NMC/LMO	195 mm x 145 mm	151k
	B	NMC	195 mm x 125 mm	153k

Table 1: Cell characteristics for experimental benchmarking study.

- 2 types of cells
- Various electrical cycling experiments
 - Quick tests : transient response
 - Longer tests: coupling between thermal and electrochemical

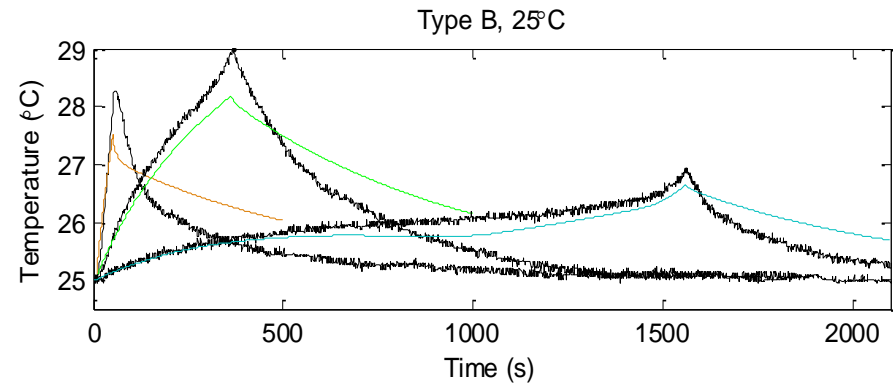
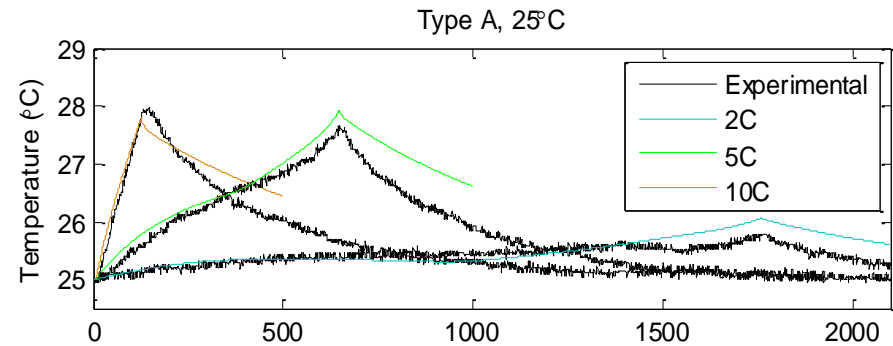
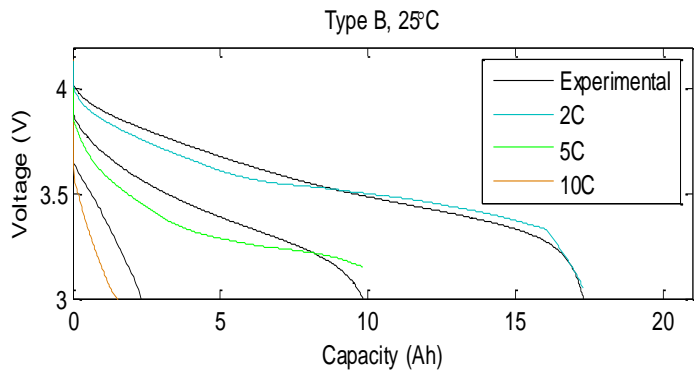
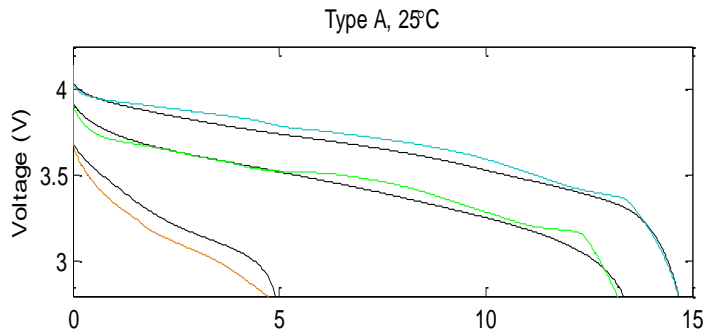


Simulation/experiment
voltage error for different
SOC for each cell

HPPC tests at different current
magnitude (different SOC)

Multi-rate capacity test validation

Experiments on longer time scale => the temperature effects are more important



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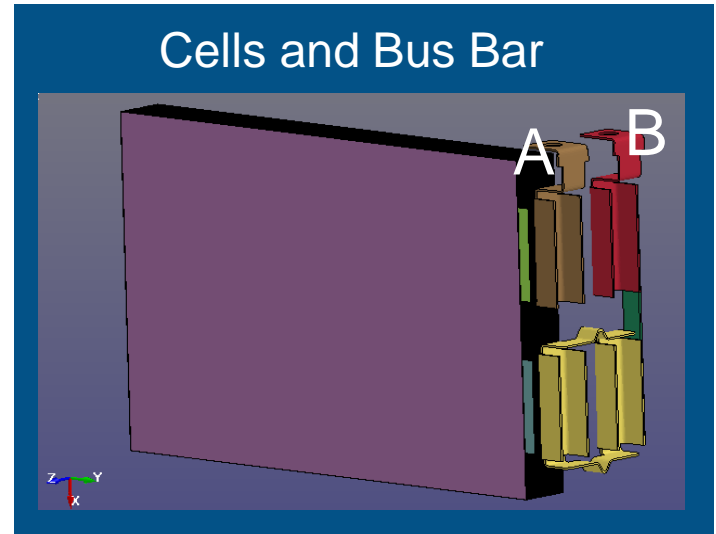
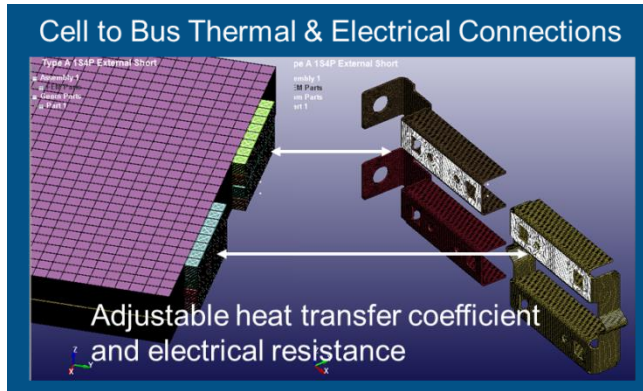
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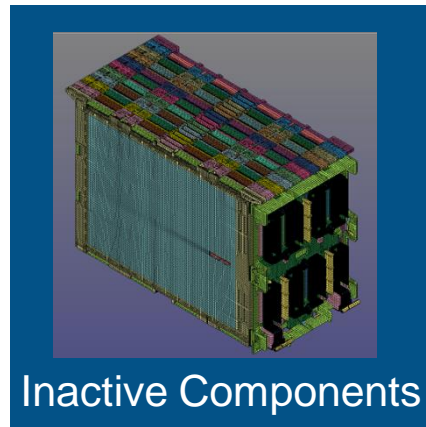
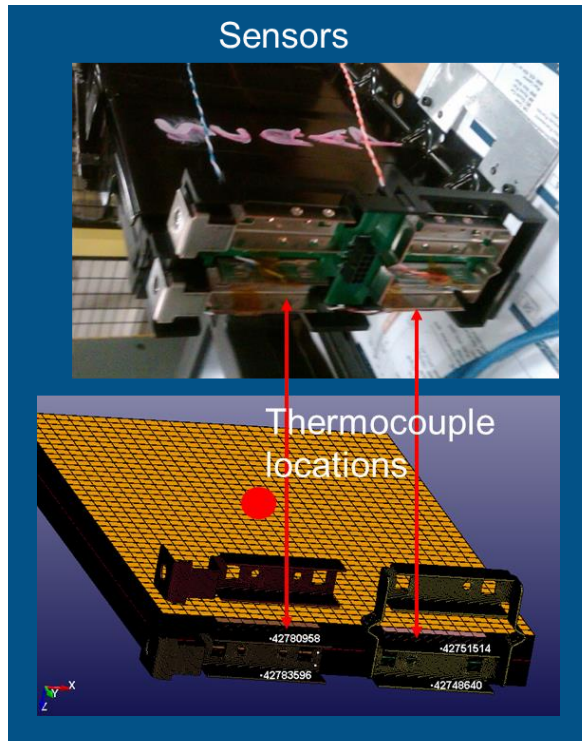
External Short Model Setup



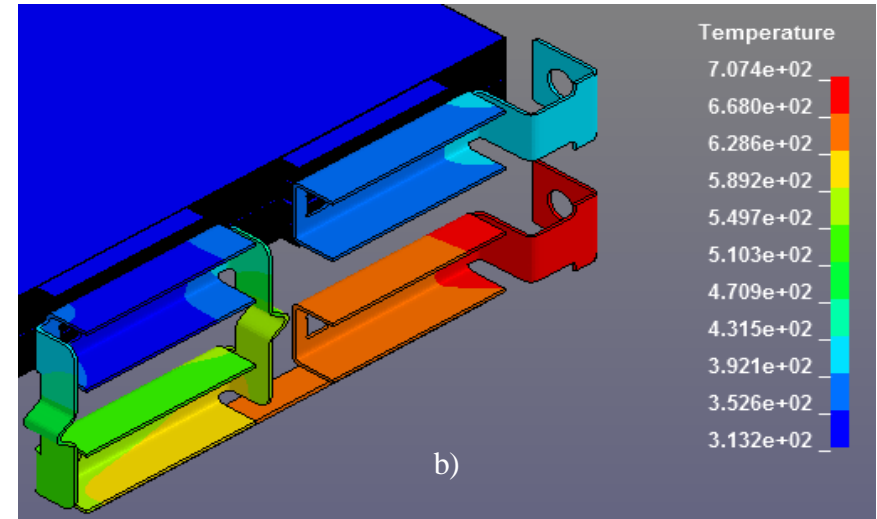
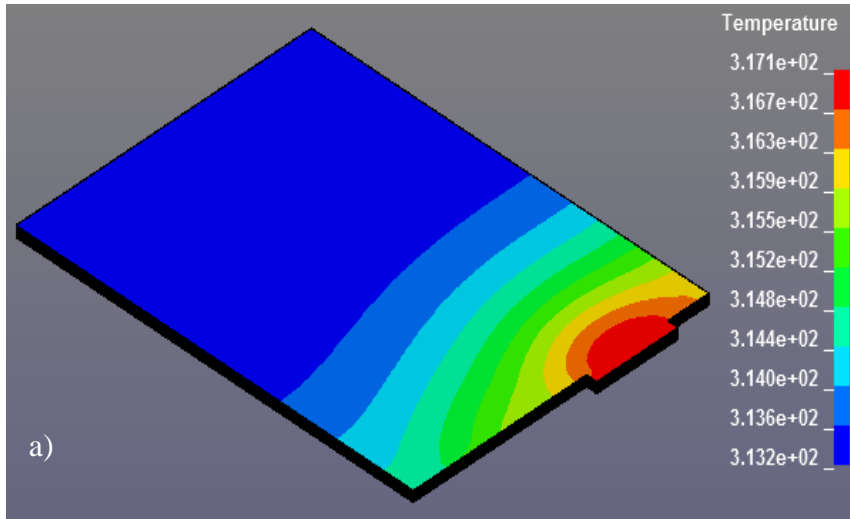
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Short circuit resistance applied between A and B creates current pathway



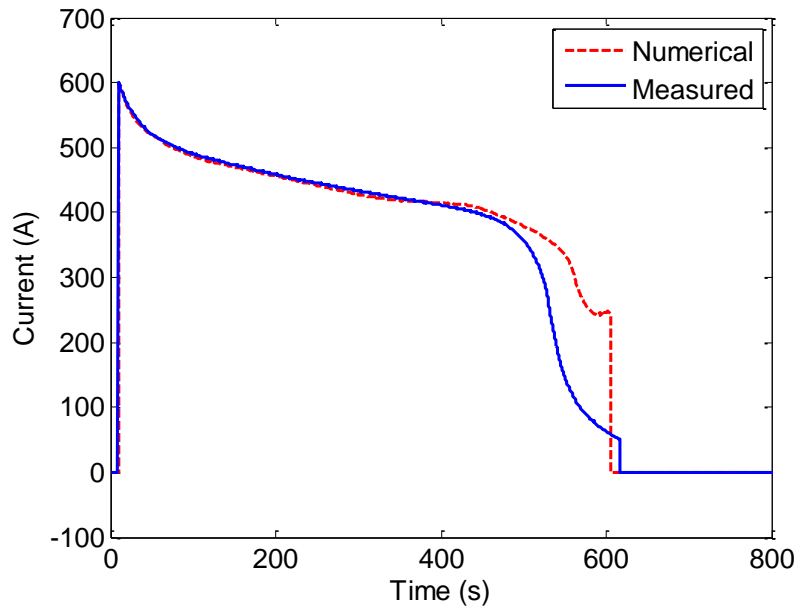
External Short Thermal Fringe Plot



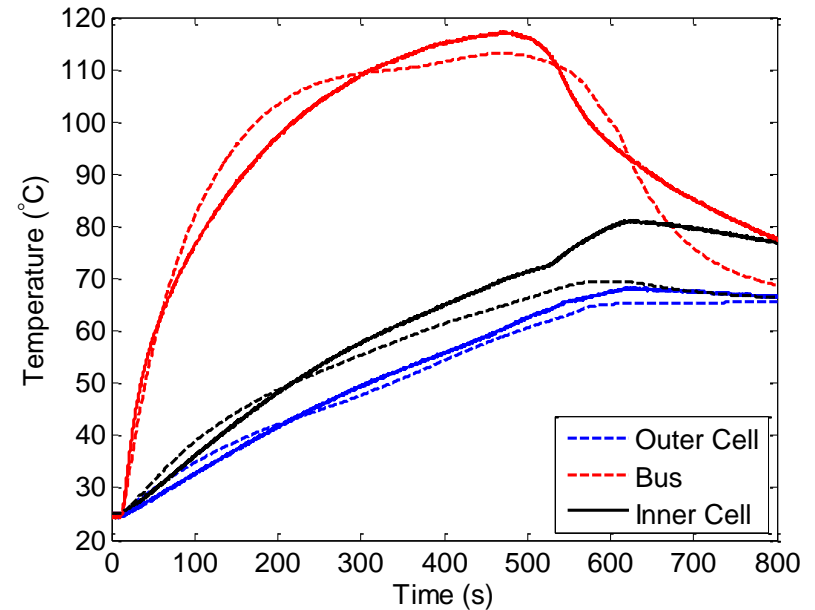
- Average short resistance is 6.5 mOhm, equivalent to $\sim 2 \text{ mm}^2$ steel connection across terminals
- Heat propagates from bus to cells; higher bus temperatures observed where cells are not connected.

External Short Circuit Validation

Model Predicted Current versus Experiment



Model Predicted (Dashed) Temperatures versus
Experiment (Solid)



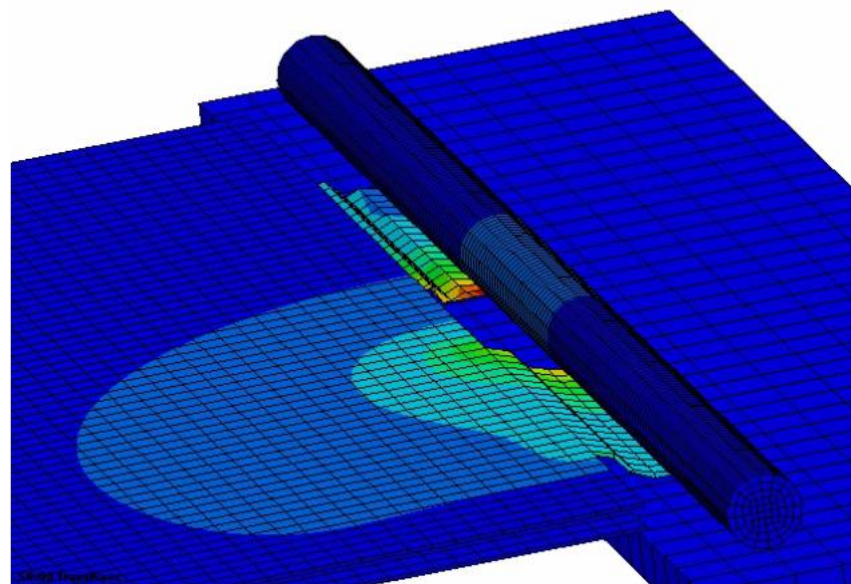
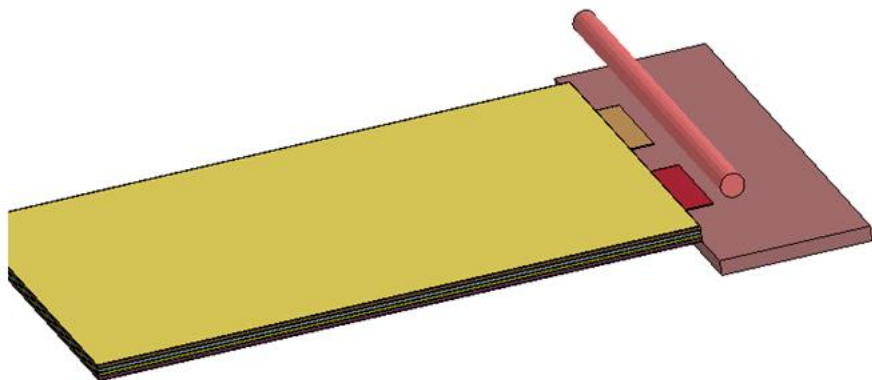
- Good agreement between numerical and measured data for electrical variables
- Thermal predictions demonstrate agreement of 5-10 °C between numerical and experimental data (excluding >550 s for inner cell)



External short example 2



Conducting cylinder falling
on the tabs of a cell creates
an external short

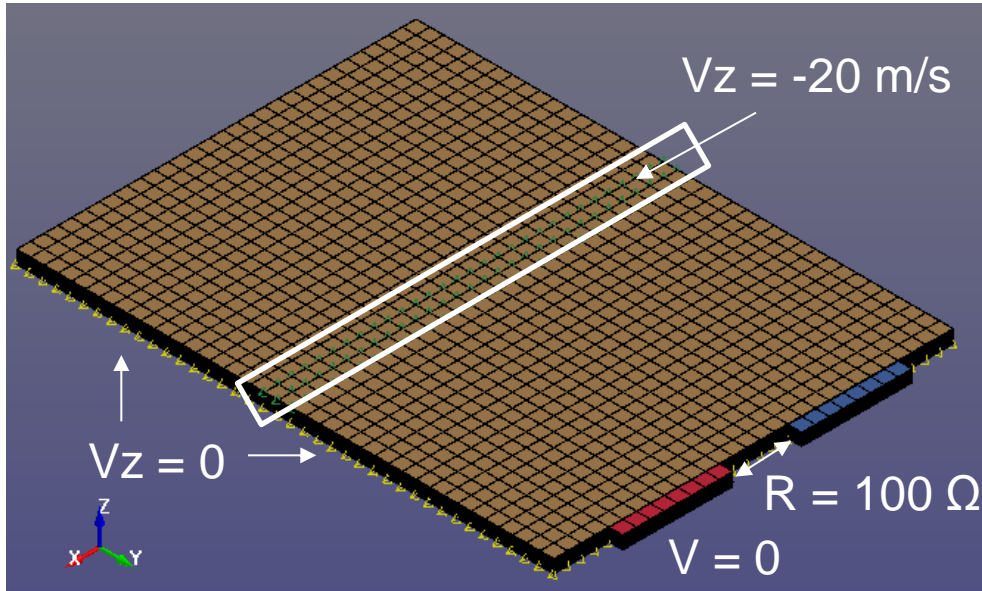


50.00 frame/sec

- Li-ion cell in an electric car
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- **Presentation of internal short cases**

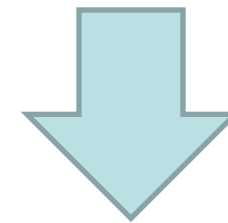
Internal short case 3 Cell Crush Case Study

Boundary Conditions



- Thermal boundary conditions same as previous simulations
- Failure criteria is unit cell compressive strain threshold
- Randles circuits replaced by direct short once failure criteria is exceeded

Mech + Electrical + Thermal
 $t_f = 50 \mu s$
 $dt = 0.2 \mu s$



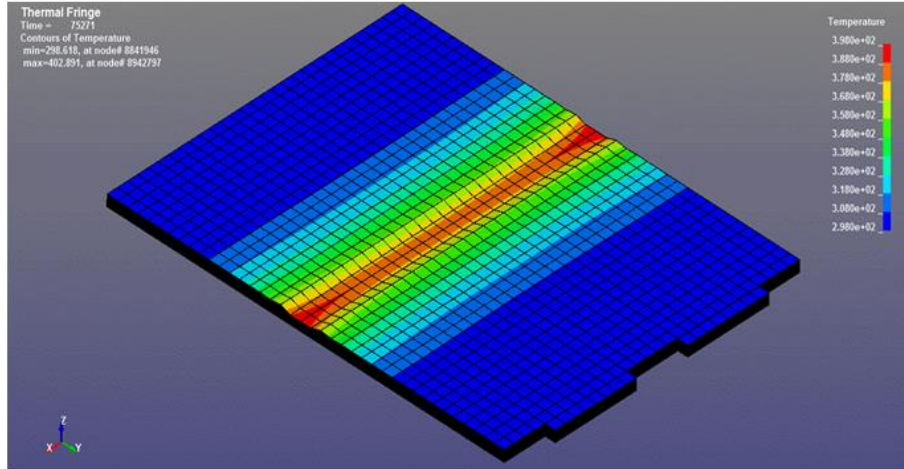
“Freeze”
mechanics

Electrical + Thermal
 $t_f = 50 s$
 $dt = 1 s$

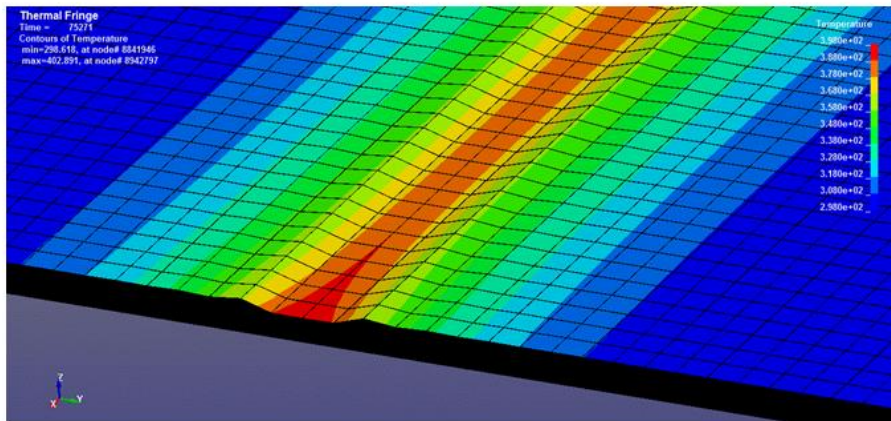
Internal short case 3

Cell Crush: Thermal results

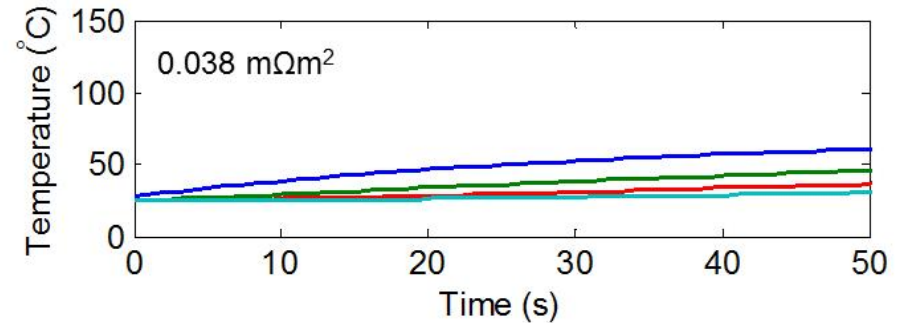
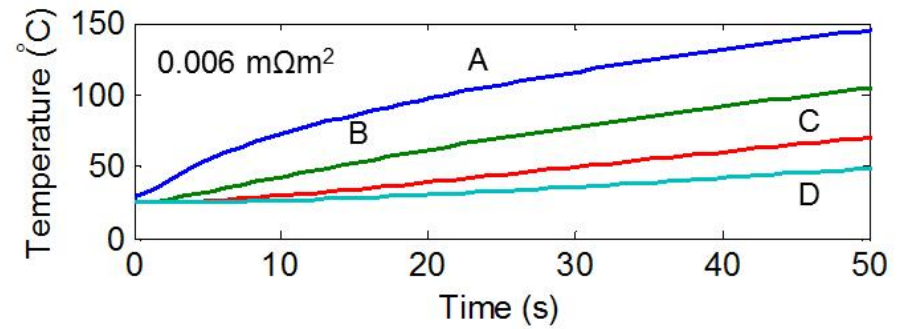
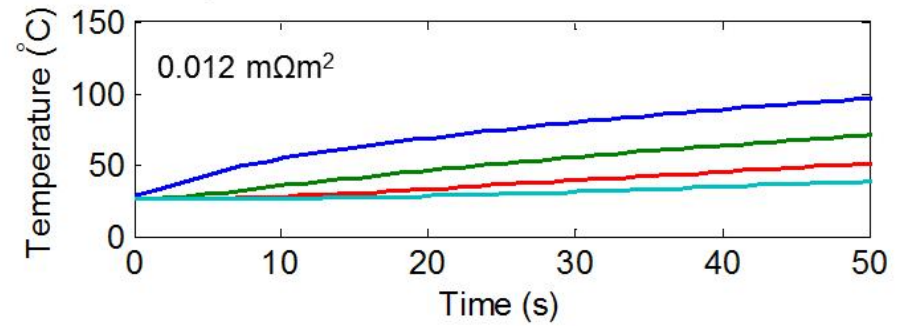
Thermal Fringe Plot



Thermal Fringe Plot Zoomed



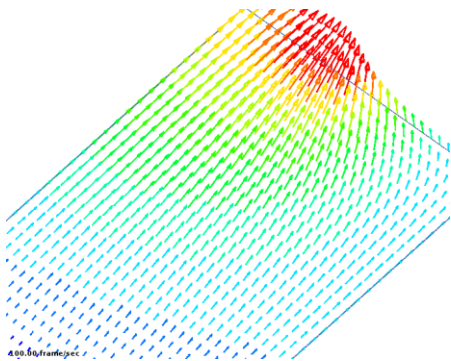
Temperature of Cell Surface versus Time



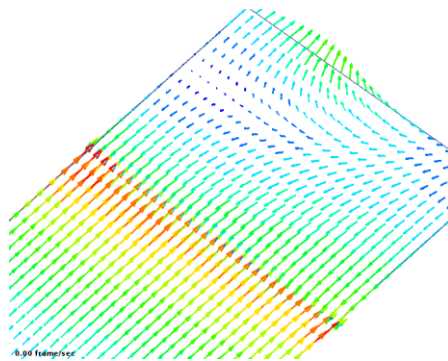
A: center of crush; B: 10 mm from center
 C: 20 mm from center; D: 30 mm from center

Current Density Vector Plots

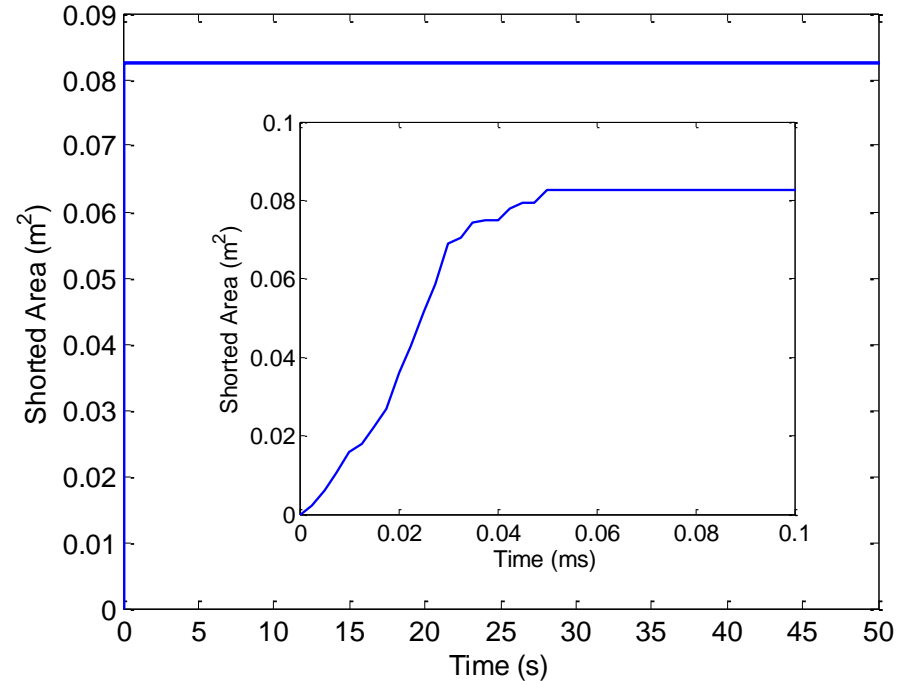
Before Internal Short



After Internal Short



Shorted Area versus Time

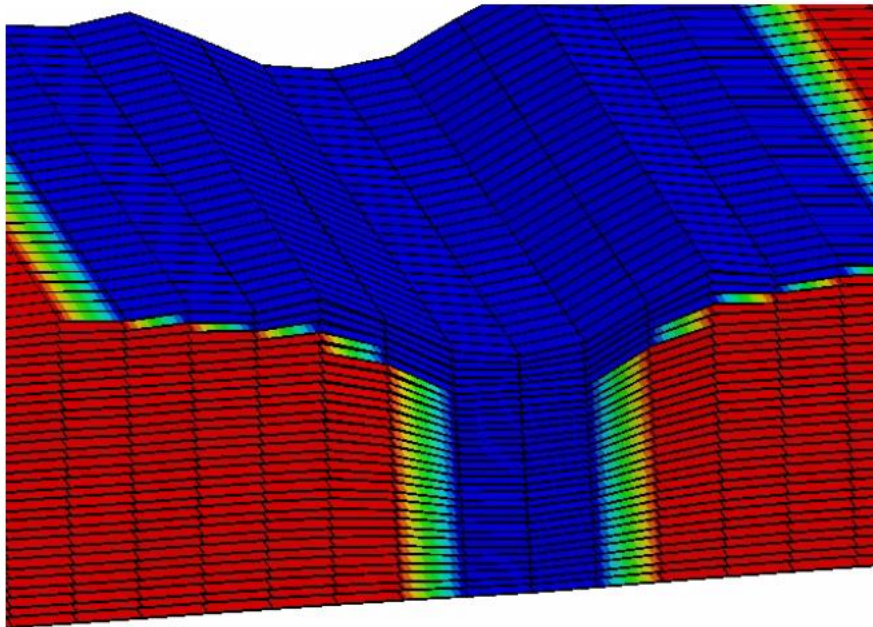


Shorted area increases upon application of external load, then stabilizes
Resistivity combines with shorted area to compute corresponding current response



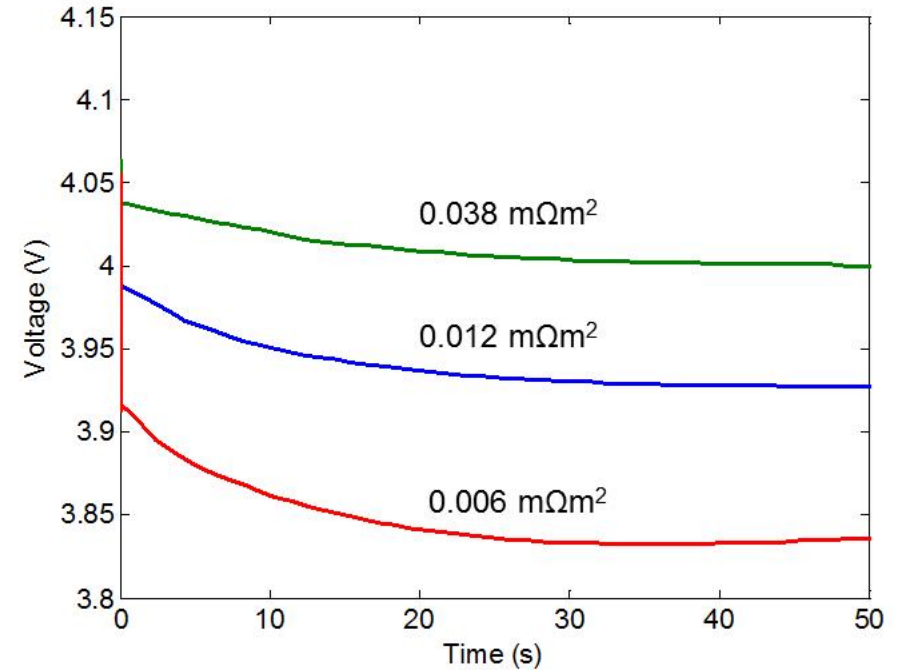
Cell Crush: Electrical results

SOC Fringe Plot



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Terminal Voltage versus Time



*Charge depletion occurs locally, then proceeds globally, with corresponding heat generation
Voltage drop increases with decreasing short resistivity*

Summary

- A three-dimensional finite element model has been developed for battery abuse case studies
- The model is parameterized using benign experiments on cells and cell components
- The model is available on solid and thick shells as a beta version
- Validation activities are underway

Future Work

- Add a “Battery packaging” in LS-PREPOST to easily create the models
- Extend the model to composite thick shells
- Develop higher-fidelity failure models and examine more complex loading conditions
- Improve models for short resistance, based on comparisons with experiments
- Replace empirical inputs with an increasingly analytical approach